Numerical analysis in biofluid dynamics: eye, nose and blood vessels

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2 Analysis of the human eye

- Rhegmatogenous retinal detachment
- Analysis of healing after corneal transplantation

Biodegradable vascular prostheses



Assessing virtual surgeries of the human nose via computational fluid dynamics

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Anatomy and functioning



It the nose flow important?

- $\bullet\,$ At least 1/3 of the adult world population is troubled with nasal breathing difficulties^1
- In 2014, the one-year (only!) cost of cronic rhinosinusits (alone!) in US (only!) was $22bn^2$
- Certain nose surgeries have 50% failure rate³

Very large margin for improvement

¹Stewart et al. Int J Gen Med 2010
²Smith et al. The Laryngoscope 2015
³Sundh & Sonnergreen, Eur Arch Otholaringol 2015

The workflow

- Segment the CT scan
- 2 Construct a volume mesh
- Compute the CFD solution (DNS, LES, RANS, ...)



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How to proceed?

Bringing CFD into the **clinical** setting requires:

- Assess reliability through a solid benchmark
- Extract CFD-derived information that is useful to surgeons

The benchmark

Reliability

- An unique Reynolds number does not exist
- Most authors use RANS, but the flow is not turbulent
- Most authors use steady RANS, but the flow is low-Re and unsteady
- Geometry created from CT scan not unique

Ongoing

- tomo-PIV experiment being developed at OTH Regensburg
- An ad-hoc DNS solver has been developed at Polimi (IMB, fast)

How to extract useful information

The lack of the functionally normal nose

CFD solution alone does not help surgeons to find the best surgery

- Main reason: lack of functionally normal reference nose
- Shape optimization, but an objective function is lacking (well-being?)
- Strong inter-subject anatomical variations with different functional significance
- How do we compare 2 anatomies? Ex. pre-op and post-op

Purpose

- Compare pre-op and post-op, HOW?
- Compare 2 healthy anatomies, HOW?
- Neglected in the literature
- Goal: show that comparison criterion affects the results



Method

- Compare pre-op and post-op
- Endoscopic Medial Maxillectomy (EMM)

3 conditions:

- CPG (Δp)
- CFR (*Q*)
- CPI (Power= $\dot{Q}\Delta p$)

Flow model:

- Large Eddy Simulation (LES)
- Mesh: pprox 15 million cells
- 1.5 seconds (768 processors, 24 hours)



Results: pre-op



same results in all cases: CPG, CFR CPI

Results: post-op, difference between CPG and CFR



VERY large localized differences

Results: comparing global values

flow forcing	CPG		CFR		CPI	
cases	pre-op	post-op	pre-op	postop	pre-op	post-op
$\dot{Q} imes 10^4[m^3/s]$	2.67	3.12	2.67	2.67	2.67	2.95
p _{thr} [Pa]	-24.45	-24.45	-24.52	-18.50	-24.45	-22.14
Power $ imes 10^3 [W]$	-6.53	-7.63	-6.55	-4.94	-6.53	-6.53
variation in [%]	$\Delta \dot{Q} = 16.9\%$		$\Delta \dot{Q} = 0\%$		$\Delta \dot{Q} = 10.5\%$	
	$\Delta p_{thr} = 0\%$		$\Delta p_{thr} = -24.6\%$		$\Delta p_{thr} = -9.5\%$	
	$\Delta Power = 16.9\%$		$\Delta Power = -24.6\%$		$\Delta Power = 0\%$	

VERY large differences in GLOBAL quantities

Conclusions

- The flow forcing choice is crucial
- Large differences in GLOBAL quantities
- Large differences in LOCAL quantities
- Worst choice is CPG (geometry dependent)
- CPI or CFR? consensus among clinicians is still to be established.

OpenNOSE community

- Active since 2011, Website (www.open-nose.org) launch 2023
- Multi-disciplinary (\approx 30 people), Polimi leader
- Driven by clinical problems and ENT surgeons
- Aim: develop virtual surgery, support to surgeons
- DNS, experimental data, anatomy data will be freely available

Towards virtual surgery of the nose

Acknowledgement to the OpenNOSE gang



Anatomy and functioning of the eye

Anterior chamber flow

- production/drainage
- myosis/mydriasis
- buoyancy-driven
- saccades

Vitreous chamber flow

- sub-retinal
- saccades



Retinal detachment



Posterior vitreous detachment (PVD)

- more common in myopic eyes;
- preceded by changes in vitreous macromolecular structure reasons.
- If the retina detaches \rightarrow loss of vision;

Rhegmatogeneous retinal detachment:

• fluid enters through a retinal break into the sub retinal space and peels off the retina.

Risk factors:

- myopia;
- posterior vitreous detachment (PVD);
- lattice degeneration;
- ...

Investigations

Computer modeling of Rhegmatogenous Retinal Detachment

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Published: Journal of Fluids and Structures, 2018; 82:245–257 Journal of Fluids and Structures, 2022; 115:103766

Purpose

- 1 in 10,000 of the population
- Caused by retinal breaks in the peripheral retina
- Unchecked RRD is a blinding condition
- Postulated that saccadic eye movements create liquefied vitreous flow in the eye, which help to lift the retina
- Experience says that the hole condition detaches quicker than the free flap condition
- Objective: investigate if hole or free flap has larger tendency to detach

Method I



Method II



Fluid flow

$$\begin{cases} \frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla \rho + \frac{1}{Re} \nabla^2 \mathbf{u} + \mathbf{f} \\ \nabla \cdot \mathbf{u} = \mathbf{0} \end{cases},$$

For the slender 1D structure

$$\frac{\partial^{2}\mathbf{X}}{\partial t^{2}} = \frac{\partial}{\partial s}\left(T\frac{\partial\mathbf{X}}{\partial s}\right) - \frac{\partial^{2}}{\partial s^{2}}\left(\gamma\frac{\partial^{2}\mathbf{X}}{\partial s^{2}}\right) + Fr\mathbf{g} - \mathbf{F}$$

Method III

Wall motion (Repetto et al. (2005)), angles tested 8° , 15° , duration 0.045 s



All data from the literature

- Retinal thickness 70 μ
- Youngs modulus from measurements
- Liquid similar to water
- Varying: L, θ and Δ

Dynamics for retinal tear

L=2 mm, $\theta = 33.6^{\circ}$



Dynamics for retinal hole

L=2 mm, $\theta = 33.6^{\circ}$, $\Delta = 0.17$ mm

Movie 2

Winkler theory



$$d=\max(v|_{s=0},0)=\max(rac{lpha M_{c}+F_{c,n}}{2lpha^{3}\gamma},0),$$

where α is the ratio between the soil spring rigidity k_T and foundation beam stiffness γ .

d is the tendency to detach

Different filament lengths L*: maximum tendency to detach

clamping angle $\theta = 33.56^{\circ}$, $\Delta^* = 0.17mm$ (retinal hole) 15 degree saccade, 8 degree saccade



Increasing L^* increases the maximum value of $d_{0,max}$

Biofluid dynamics

Different clamping angles θ : maximum tendency to detach

length $L^* = 2$ mm, $\Delta^* = 0.17mm$ (retinal hole) 15 degree saccade, 8 degree saccade



Tear

Hole

A maximum value of d_{max} is found

d_{max}

Comparison horseshoe tear & hole: maximum tendency to detach

clamping angle $\theta = 33.56^{\circ}$, $\Delta^* = 0.17 mm$ (retinal hole)



The retinal hole is more prone to detach compared to horseshoe tear

The main results, for GRT and RH using realistic parameter values, show:

• Increasing *L*^{*} increases the tendency to detach (both GRT & RH).

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- Changing Δ^* , the hole size, has little effect on the tendency to detach for both saccades tested.

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- Changing Δ^* , the hole size, has little effect on the tendency to detach for both saccades tested.
- **RH** vs **GRT**, the tendency to detach of a RH, compared to a GRT, is 2-3.5 times larger for retinal flaps of 1.5-2.5 mm, and the ratio increases for longer flap lengths. This ratio increases as the saccadic amplitude is increased.

Optimization of patient positioning for improved healing after corneal transplantation

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Published: Translational Vision Science & Technology, 2019; 8(6):9 Submitted: Journal of Biomechanics, 2022

Purpose I

Corneal endothelial cell dysfunctions

- Fuchs' endothelial dystrophy (up to 11% of US population above 40 years)
- Congenital hereditary endothelial dystrophy
- Corneal edema due to complications from other types of eye surgery



Purpose II

DMEK procedure (about 15 minutes)



Post-operative problem

• graft peal off, mostly in lower quadrant (> 20% of cases)

Objective

• Analyse optimal patient positioning for improved healing

Method I

Compute stationary solution of air bubble in aqueous humor (pprox water) solving

11 0

- incompressible Navier-Stokes equations...
- coupled with transport equation for phase fraction γ (VOF)

$$\rho \frac{\partial U}{\partial t} + \rho U \cdot \nabla U - \mu \nabla^2 U = -\nabla p_d - \rho g \cdot x + \sigma \kappa \nabla \gamma,$$

$$\frac{\partial \gamma}{\partial t} + \nabla \cdot (U\gamma) + \nabla \cdot [U_r (1-\gamma)] = 0,$$

Important parameters

- anterior chamber shape
- surface tension
- static contact angles (our measurements)
- densities
- gravitational acceleration

LESS Important parameters

viscosities

Method II



Parametric study

- ACD
- with and without natural lens
- gas fill (time)
- patient position

Method III



Measurements

- gas-graft coverage in %
- gas exposure on graft over time

-4 -6

-5

0 [mm] No exposure

5

Results I

Gas-graft coverage



Results II

Patient position that maximises gas-graft coverage



Results III

Mean graft coverage changing patient position over time



Results IV

Gas exposure on graft over time: Optimal versus Random patient positioning



- Patient positioning is negligible if ACD is small
- Optimal patient positioning important only for larger ACD
- Exposure (position of gas bubble) more sensitive than Coverage (%) w.r.t. patient positioning

Engineered small-diameter vascular prostheses: a study in bioreactor

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> Submitted: Journal of Biomedical Materials Research Part A, 2022

Motivation

- Current strategies for aterosclerosi is substitute with bioprotesi
- Available protesi are D > 7mm (eg. Dacron)
- Goal: produce engineered bioprotesi D < 6mm



Method I



Method II

Modelling of fluid dynamics

- Predictive tool: experiments are long and costly
- Detailed results difficult to obtain experimentally
- Step-by-step:
 - Newtonian steady state
 - 2 Newtonian unsteady (heart beat)
 - Son-newtonian (similar to blood) unsteady

Method III

Newtonian steady state

- Incompressible flow
- Pipe geometry with smooth walls
- Steady state

Solution is analytical

$$\tau_W = -\mu \frac{8U}{D}$$

Results I



Biodegradable vascular prostheses

Results II



Ongoing

Newtonian unsteady

- Incompressible flow
- Pipe geometry with smooth walls
- Unsteady (signal from heart beat)

Solution is analytical

$$\tau_{W} = real\left\{\sum_{n=1}^{N} P_{n}^{\prime} \frac{R}{\Lambda_{n}} \frac{J_{1}(\Lambda_{n})}{J_{0}(\Lambda_{n})} e^{in\omega t}\right\}$$

where Λ_n depends on the Womersly number (non-dimensional frequency)



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