

**GMA08 – Riunione Gruppo Materiali AIMeTA**  
*Genova, 29 Febbraio - 1 Marzo 2008*

**RESIDUAL THERMAL STRESSES IN A  
PERIODICALLY COATED ANISOTROPIC LAYER**

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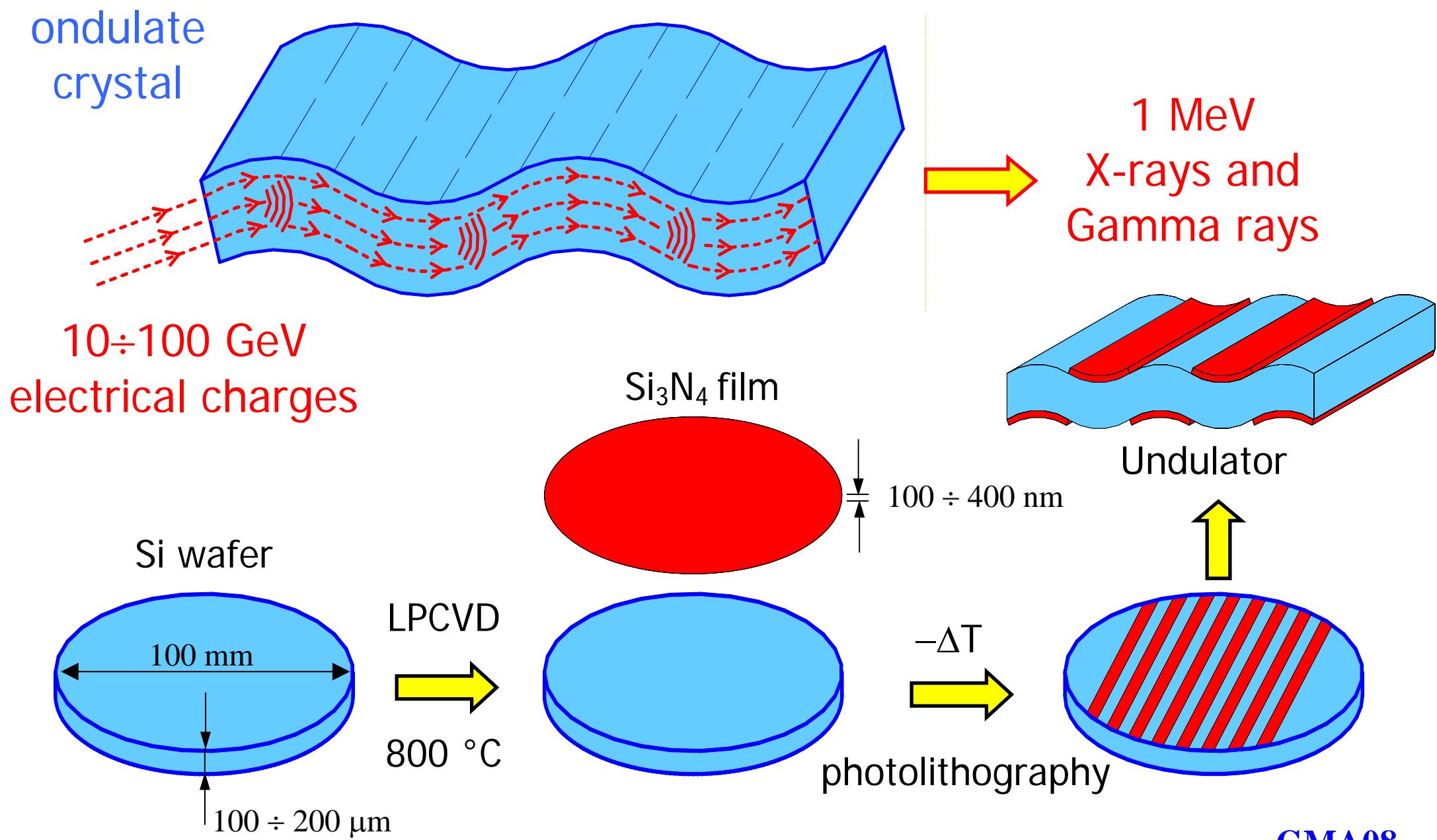


UNIVERSITA' DEGLI STUDI  
DI MODENA E REGGIO EMILIA

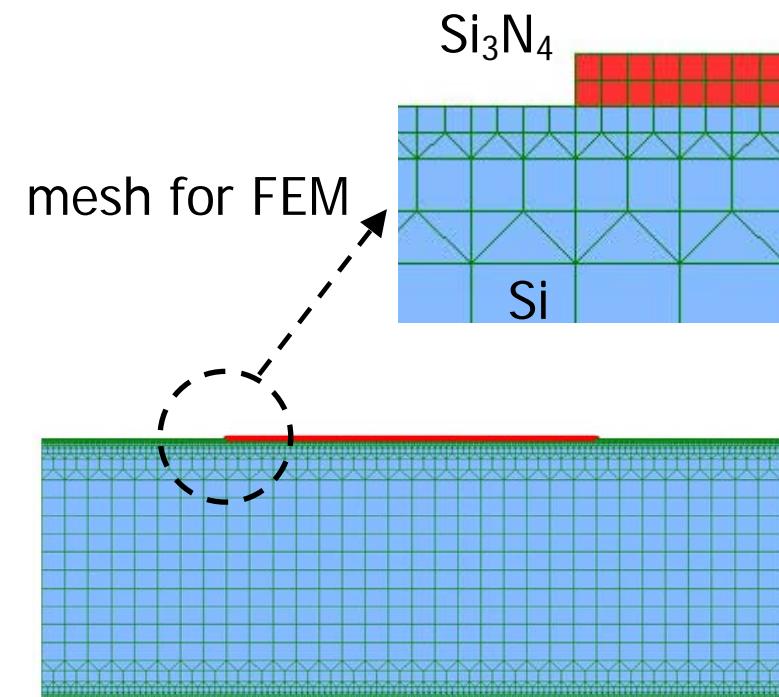
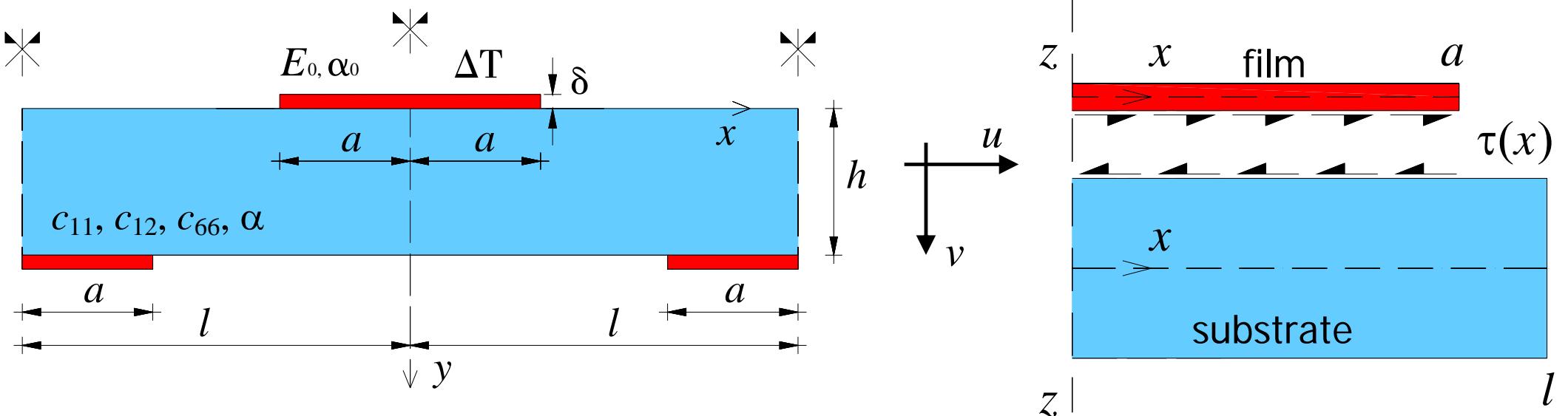
Dipartimento di Scienze e Metodi dell'Ingegneria

**GMA08**

# Crystalline undulator



# Analytic and FEM model



**boundary conditions:**

- $u(0, y) = u(\pm l, y) = 0, \quad \tau(0, y) = \tau(\pm l, y) = 0, \quad \text{for } 0 \leq y \leq h,$
- $\sigma_y(x, 0) = \sigma_y(x, h) = 0, \quad \text{for } |x| \leq l,$

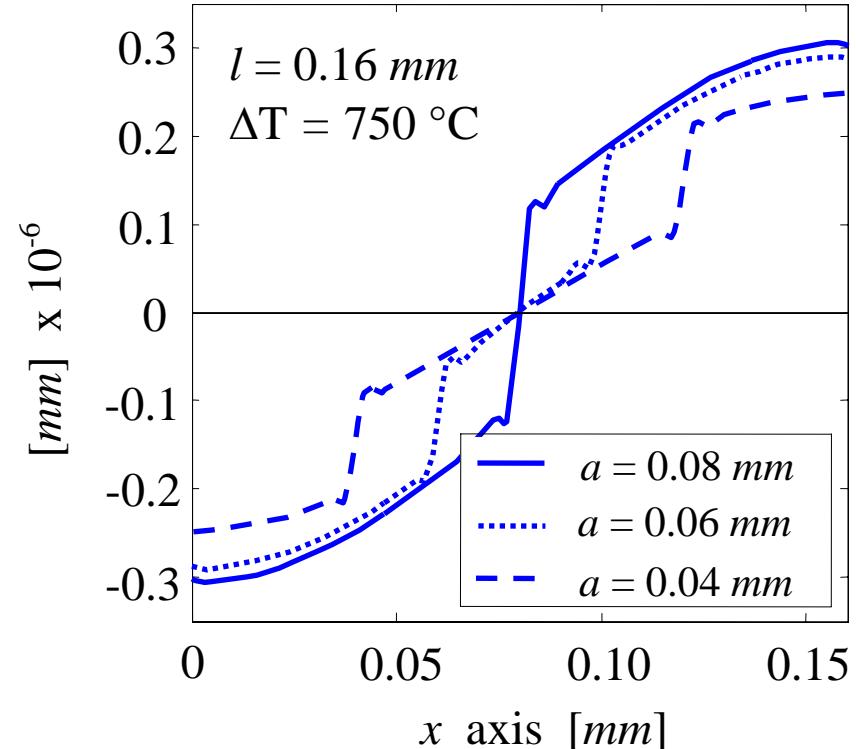
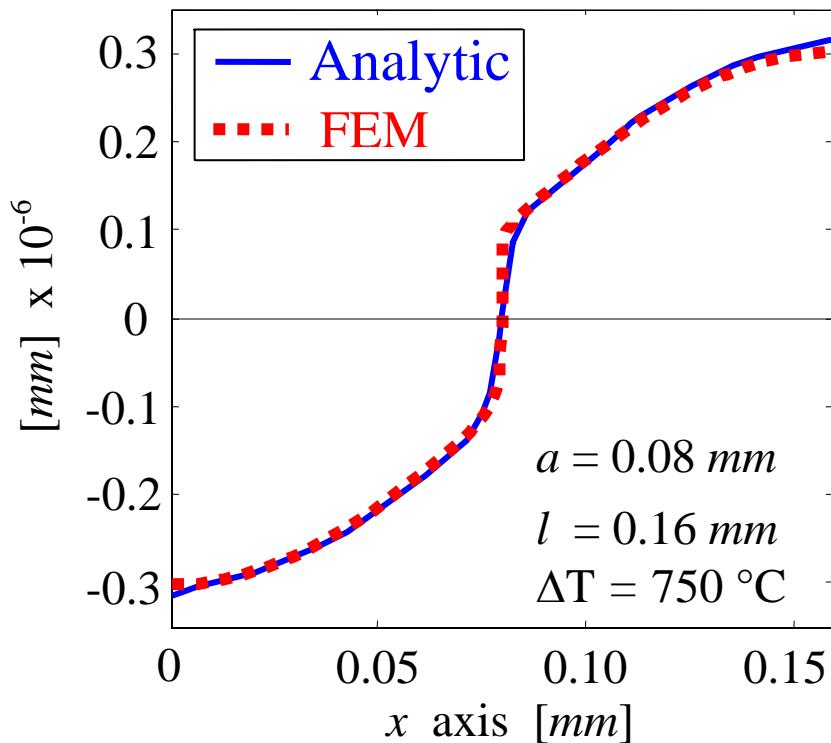
**adherence condition:**

$$u(x, 0) = u_0(x), \quad \text{for } |x| \leq a; \quad u(x, h) = u_0(x) \quad \text{for } (l - a) \leq |x| \leq l$$

**displacement field:**

$$u(x, y) = \sum_{n=1,3}^{\infty} U_n(y) \sin(n\pi x), \quad v(x, y) = \sum_{n=1,3}^{\infty} V_n(\bar{y}) \cos(n\pi x).$$

# Vertical displacement $v(x, 0)$



## Future aims

- Take into account the variation of the mechanical properties of the deposited film (FGM film),
- take into account the microstructural effect (e.g. by using couple stress theory).